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# Slope Length Calculations from a DEM within ARC/INFO GRID

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#### Abstract:

The Universal Soil Loss Equation has been used for a number of years to predict soil erosion rates. One of the required inputs to this model is the cumulative uphill slope length. Calculating it has been the largest problem in using the USLE. The only necessary data for this calculation is a digital elevation model (DEM). DEMs have been available for years and are frequently used within Geographical Information Systems (GIS), but until recently, the GIS software has not been robust enough to support the necessary calculations. This paper describes a method for calculating slope length from a digital elevation model within the ARC/INFO GRID raster system.

**Keywords**: Erosion, geographical information systems, slope, slope length, Digital elevation model.

#### **Erosion Modeling**

The USLE (universal soil loss equation) has been used for a number of years to predict

soil erosion rates. In its traditional form, the USLE is given by the following equation:

#### A = RKLSCP

where A is the average annual soil loss per unit area, R is the rainfall and runoff factor, K is the soil erodability factor, L is the slope length factor, S is the slope steepness factor, C is the cover and management factor, and P is the support practice factor (8). This paper will focus on generating the L and S factors from a DEM (digital elevation model) within GRID, the raster module of the GIS software package ARC/INFO. The two inputs to the LS factor are cumulative slope length and slope angle.

In recent years, soil erosion models more advanced than the USLE have been created, including ANSWERS (1), AGNPS (9), and the USLE's replacement, RUSLE (6). It is important

to note here that RUSLE and AGNPS include both a slope and a slope length component in their equations.

Generating the LS values poses the largest problem in using the USLE (4, 5, 6), especially when applying it to real landscapes within a GIS (4). Traditionally, the best estimates for L were obtained from field measurements, but these are not always available or practical. In addition, until recently, GIS packages have not been able to support the algorithms necessary for slope length calculations. This software limitation can be overcome using ARC/INFO GRID, a raster-based modeling environment and ARC/INFO's Arc Macro Language (AML) programming environment (2).

Calculating slope from a DEM is relatively simple, but care must be taken when selecting an algorithm. For example, the ARC/INFO GRID command, **SLOPE**, calculates maximum slope from a 3X3 cell neighborhood, not a maximum downhill slope (2). The AML program **dn\_slope.aml** given at the end of this paper calculates maximum downhill slope.

#### Algorithm Description:

The overall methodology is described in Figure 1. The first requirement for the algorithm is a depressionless DEM. We have found that the GRID command **FILL** does not eliminate all depressions. Therefore, we have written a small AML (**fil.aml**) which is similar to the **FILL** command (2) but will entirely fill all the depressions in a DEM.

Once this has been completed, the maximum downhill slope and the flowdirection can be calculated using the AML **dn\_slope.aml** and the GRID command **FLOWDIRECTION**. It is important to note here that the flowdirection and the direction of maximum downhill slope are the same.

High points are designated (**high\_pts.aml**) by selecting those cells which have either no flow entering them or in cases where both the cell in question and its input cell have a slope angle of zero.

Non-cumulative slope length (NCSL) is then calculated for each cell within **sl.aml**. In short, the distance to each cell from its input cell is calculated using the following equations:

if the cell being calculated is a high point

NCSL = 0.5(cell resolution)(atan $\beta$ ).

if the input cell is in a cardinal direction (N, S, E, W),

NCSL = (cell resolution) (atan  $\beta$ )

otherwise,

NCSL = 1.4142(cell resolution)(atan $\beta$ ).

( $\beta$  is the slope angle)

This is based on the assumption that the calculations for slope length are from the center of the cell to the center of its input cell. Therefore, as high points do not have an input cell, the 0.5 value represents only the erosion occurring within the half of that cell which is uphill of the center point.

At this point, all the input coverages are present to calculate cumulative slope length (NCSL, slope angle, high points, and flowdirection). This is done by simply summing the noncumulative slope lengths along flowdirection beginning at the high points (**s\_length.aml**). There are a number of assumptions built into this calculation. The first is that in areas of converging flows, the highest cumulative slope length takes precedence. The second is in finding cells in which there is no erosion. The assumption here is that if the slope angle decreases by 50% (or more) from one cell to the next along flowdirection (i.e. 10° to 5°), there is net deposition rather than erosion. This is similar to assumptions made in other studies (4 and 7), although in these cases, the cutoffs were a change of 50% from the average uphill slope angle and a change of 50% from the maximum uphill slope angle, respectively. While we do not consider more than the nearest upslope cell in our cutoff calculations, the program allows the user to specify any cutoff value (50% will be the default).

The final steps in this analysis are to convert the cumulative slope length values into feet (if necessary) and to calculate the LS values. The USLE equation for LS values is:

$$LS = (\lambda/72.6)^{m} (65.41 \sin^{2}\beta + 4.56 \sin\beta + 0.065)$$

where  $\lambda$  is the cumulative slope length,  $\beta$  is the downhill slope angle, and m is a slope contingent variable--0.5 if the slope angle is greater than 2.86°, 0.4 on slopes of 1.72° to 2.86°, 0.3 on slopes of 0.57° to 1.72°, and 0.2 on slopes less than 0.57° (8).

The ARC/INFO AML program that calculates the LS values requires a DEM coverage and two input values: the cell resolution units (feet or meters) and the decrease in slope angle required for identifying cells with net deposition rather than erosion (a 50% decrease is the default). A simple user interface (**slmenu.aml**) has been programmed to assist the user in entering these required values. The final outputs from this program are three coverages: ls\_values (USLE LS values), slope\_angle (downhill slope angles), and slope\_len (the cumulative slope lengths).

The overall flow of the AMLs begins as follows: **slmenu.aml** calls the user interface AML **execute.aml**. Once the user has input the appropriate information, **sl.aml** takes over. For the rest of the LS calculations, **sl.aml** acts as the core program and calls the other AMLs as necessary. It is important to note here that the only programs that are designed to act independently are those that effectively replace ARC/INFO commands (**fil.aml** and **dn\_slope.aml**).

#### **Model Limitations**

The first problem associated with using a DEM to calculate slope length is the typically low resolution (i.e. 30m for USGS DEMs). Microfeatures which slow runoff, and therefore erosion, are lost. Thus, LS estimates will be higher than actual values. As DEM resolutions get higher, the landscape will be more accurately modeled, and erosion estimates will approach actual values. However, in cases where detailed field studies are impractical, this method offers a solution with available data.

The second limitation is directly associated with the model presented. For accurate cumulative slope length values, the high points calculated by the model must correspond to true

terrain high points. To accomplish this, this model must be run on a watershed scale, not on partial watersheds. If this is not done, slope lengths will be underestimated because the high points calculated may be located on the sides of slopes, not on ridgelines. It is important to note here that the Arc/Info GRID command **WATERSHED** will delineate watersheds from a DEM (2).

#### **Conclusions**

While field estimates of cumulative slope length may be more accurate than this model, for larger areas they are typically not practical nor affordable. In addition, trained personnel may not be available. Thus, cumulative slope length calculations from a DEM may be the only option if erosion rates are to be modeled. The advantages of this model are:

1) Using the USLE, erosion rates can be calculated entirely within a GIS environment.

2) The cumulative slope length output can be used in a number

of different erosion models, including the USLE, RUSLE, and AGNPS (8,6,9).

3) The erosion rates coverage can be used within the GIS as an

input to land suitability analysis problems. For example, erosion rates may be one factor considered when deciding which parts of a large superfund site should be reclaimed.

4) Erosion rates can be calculated for large areas without timeconsuming and costly slope length field surveys.

Finally, we would like to state that the AMLs provided at the end of this paper represents a prototype implementation of the method for calculating slope length from a DEM within a GIS environment, not a definitive solution. References:

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 Department of Agriculture, Conservation Research Report 35, 80 p.

```
slmenu.aml
&terminal 9999
&menu sl.menu &position &UL &stripe 'Slope Length'
&return
                     execute.aml
&severity &warning &routine error
&severity &error &routine error
&sv error = .FALSE.
&sv test = [exist %.DEM% -grid]
&if %error% &then
 &do
 &sv choice = \sim
  [getchoice OK -prompt 'You must choose a DEM.']
 &return
 &end
&sv test = [null %.unit%]
&if %error% &then
 &do
 &sv choice = \sim
  [getchoice OK -prompt 'You must choose a unit of measure.']
 &return
 &end
&sv test = [calc \%.cutoff\% * 1]
&if %error% &then
 &sv.cutoff = 50
&severity &warning &ignore
&severity &error &fail
&run s.aml %.DEM% slope len ls values %.unit% %.cutoff% slope angle
&delvar .DEM
&delvar .unit
&delvar .cutoff
&stop
```

sl.aml

### /\* The input : a grid of elevations. /\* The elevations must be in the same units as the horizontal distance. /\* The unit of measurement for the elevation grid. /\* The change in slope(as a %) that will cause the slope length /\* calculation to stop and start over. /\* The output: a grid of cumulative slope lengths, /\*: a grid of LS values for the soil loss equation. /\*: an optional grid of down hill slope angle. /\* Usage: sl <elevation grid> <slope length grid> <LS value grid> /\* {FEET | METER} {cutoff value} {slope angle grid} &args sl elev sl out LS out grd units cutoff value sl angle &sv .grid units = [translate %grd units%] &if [null %cutoff value%] or [index %cutoff value% #] eq 1 &then &sv .slope cutoff value = .5&else &sv.slope cutoff value = [calc [value cutoff value] / 100] setcell %sl elev% setwindow %sl\_elev% &describe %sl elev% &run fil.aml %sl elev% sl DEM sl outflow = flowdirection(sl DEM) sl inflow = focalflow(sl DEM)

&run dn slope.aml sl DEM sl slope

= [show scalar \$\$cellsize] &sv cell size &sv diagonal length = 1.414216 \* %cell size% /\* Convert to radians for cos--to calculate slope length if (sl outflow in  $\{2, 8, 32, 128\}$ ) sl length = %diagonal length% div cos(sl slope div deg) else sl length = %cell size% div cos(sl slope div deg) endif /\* Set the window with a one cell buffer to advoid NODATA around the edges \*\* setwindow [calc [show scalar \$\$wx0] - [show scalar \$\$cellsize]] ~ [calc [show scalar \$\$wy0] - [show scalar \$\$cellsize]] ~ [calc [show scalar \$\$wx1] + [show scalar \$\$cellsize]] ~ [calc [show scalar \$\$wy1] + [show scalar \$\$cellsize]] sl flow = sl outflow kill sl outflow sl outflow = con(isnull(sl flow), 0, sl flow)kill sl flow /\* The high points will have 1/2 their cell slope length for VALUE \*\*\*\*\* &run high pts.aml /\* This will be added back in after the slope lengths for all other \*\*\*\*\* sl high pts = con(isnull(sl cum l), 0, sl cum l)&run s length.aml &run Is.aml setwindow %sl elev% setmask %sl elev% setmask off kill sl (!DEM outflow inflow length high pts!) rename sl cum 1 %sl out% rename ls amount %LS out%

&if [null %sl\_angle%] &then
 kill sl\_slope
&else
 rename sl\_slope %sl\_angle%
&return

fil.aml /\* The input : a grid of elevations /\* The output: a depressionless elevation grid. /\* Usage: fil <elevation grid> <depressionless grid> &args DEM grid fil DEM %fil DEM% = %DEM grid% finished = scalar(0)&do &until [show scalar finished] eq 1 finished = scalar(1)rename %fil DEM% old DEM if (focalflow(old DEM) eq 255) { %fil DEM% = focalmin(old DEM, annulus, 1, 1) test grid = 0} else { %fil DEM% = old DEM  $test_grid = 1$ } endif kill old DEM docell finished {= test grid end kill test grid &end

&return

#### dn slope.aml

/\* The input : a grid of elevations with no depressions

/\* The output: a grid of down slopes in degrees.

/\* Usage: dn slope <elevation grid> <down slope grid>

&args DEM\_grid down\_slope

```
dn outflow = flowdirection(%DEM grid%)
&describe %DEM grid%
setwindow [calc [show scalar $$wx0] - [show scalar $$cellsize]] ~
    [calc [show scalar $$wy0] - [show scalar $$cellsize]] ~
    [calc [show scalar $$wx1] + [show scalar $$cellsize]] ~
    [calc [show scalar $$wy1] + [show scalar $$cellsize]]
/* This prevents NODATA being assigned to the edge cells that flow
 /* off the DEM. Cells that flow off the DEM will get 0 slope ***********
dn buff DEM = con(isnull(%DEM grid%), focalmin(%DEM grid%), %DEM grid%)
&sv cell = [show scalar $$cellsize]
 /* The () pervent problems that occur with using whole numbers *********
&sv cell size
             = (1.00 * \% cell\%)
&sv diagonal length = (1.414216 * \% cell size\%)
 if (dn outflow eq 64)
 % down slope% = deg * atan((dn buff DEM - dn buff DEM(0, -1)) div ~
        %cell size%)
else if (dn outflow eq 128)
 %down slope% = deg * atan((dn_buff_DEM - dn_buff_DEM(1, -1)) div ~
        %diagonal length%)
else if (dn outflow eq 1)
 % down slope% = deg * atan((dn buff DEM - dn buff DEM(1, 0)) div ~
        %cell size%)
else if (dn outflow eq 2)
 %down_slope% = deg * atan((dn_buff_DEM - dn_buff_DEM(1, 1)) div ~
        %diagonal length%)
else if (dn outflow eq 4)
 % down slope% = deg * atan((dn buff DEM - dn buff DEM(0, 1)) div ~
        %cell size%)
else if (dn outflow eq 8)
 % down slope% = deg * atan((dn buff DEM - dn buff DEM(-1, 1)) div ~
        %diagonal length%)
else if (dn outflow eq 16)
 %down slope% = deg * atan((dn buff DEM - dn buff DEM(-1, 0)) div ~
        %cell size%)
else if (dn outflow eq 32)
 % down slope% = deg * atan((dn buff DEM - dn buff DEM(-1, -1)) div ~
        %diagonal length%)
```

else %down\_slope% = 0.00 endif

&return

### 

high pts.aml

```
/* A high point is a cell that has no points flowing into it or if the only
if ((sl inflow && 64) and (sl outflow(0, -1) eq 4))
          sl cum l = setnull(1 eq 1)
else if ((sl inflow & (1, -1) \in (3, -1) (3, -1) (3, -1) (3, -1) (3, -1) (3, -1) (3, 
          sl cum l = setnull(1 eq 1)
else if ((sl inflow && 1) and (sl outflow(1, 0) eq 16))
          sl cum l = setnull(1 eq 1)
else if ((sl inflow & \& 2) and (sl outflow(1, 1) eq 32))
          sl cum l = setnull(1 eq 1)
else if ((sl inflow && 4) and (sl outflow(0, 1) eq 64))
          sl cum l = setnull(1 eq 1)
else if ((sl inflow & \& 8) and (sl outflow(-1, 1) eq 128))
          sl cum l = setnull(1 eq 1)
else if ((sl inflow & \& 16) and (sl outflow(-1, 0) eq 1))
          sl cum l = setnull(1 eq 1)
else if ((sl inflow && 32) and (sl outflow(-1, -1) eq 2))
```

&return

## <u>s length.aml</u>

```
/* Grids used from sl.aml:
  /* sl inflow
  /* sl outflow
  /* sl slope
  /* sl length
  /* sl high pts
  /* sl DEM
 /* Grid produced for sl aml:
  /* sl cum l
setmask sl DEM
nodata cell = scalar(1)
&sv finished = .FALSE.
&do &until %finished%
 rename sl cum l sl out old
 &sv counter = 0
 &do counter = 1 \& to 8
  /* Set the varibles for the if that follows
 &select %counter%
   &when 1
    &do
    &sv from cell grid
                   = sl north cell
    &sv from cell direction = 4
    &sv possible cell direction = 64
    &sv column
                 = 0
                = -1
    &sv row
    &end
   &when 2
    &do
```

```
&sv from cell grid
                     = sl NE cell
  &sv from cell direction = 8
  &sv possible cell direction = 128
  &sv column
                      = 1
                    = -1
  &sv row
  &end
&when 3
  &do
  &sv from cell grid
                    = sl east cell
  &sv from cell direction = 16
  &sv possible cell direction = 1
  &sv column
                      = 1
                    = 0
  &sv row
  &end
&when 4
  &do
  &sv from cell grid
                    = sl SE cell
  &sv from cell direction = 32
  &sv possible cell direction = 2
                      = 1
  &sv column
                    = 1
  &sv row
  &end
&when 5
  &do
  &sv from cell grid
                    = sl south cell
  &sv from cell direction = 64
  &sv possible cell direction = 4
  &sv column = 0
                    = 1
  &sv row
  &end
&when 6
  &do
  &sv from cell grid
                      = sl SW cell
  &sv from cell direction = 128
  &sv possible cell direction = 8
  &sv column
              = -1
                    = 1
  &sv row
  &end
&when 7
  &do
  &sv from cell grid
                    = sl west cell
  &sv from cell direction = 1
  &sv possible cell direction = 16
  &sv column
                      = -1
                    = 0
  &sv row
  &end
&when 8
  &do
```

```
&sv from cell grid
                             = sl NW cell
     &sv from cell direction
                               = 2
     &sv possible cell direction = 32
     &sv column
                           = -1
                         = -1
     &sv row
     &end
&end
  /* Test for possible flow source cell
if (not(sl inflow && %possible cell direction%))
  % from cell grid% = 0
  /* Test for flow source cell
else if (sl outflow(%column%, %row%) <> %from cell direction%)
  % from cell grid% = 0
 /* Test flow source cell for nodata
else if (isnull(sl out old(%column%, %row%)))
  % from cell grid% = setnull(1 eq 1)
  /* Test current cell slope against cutoff value
else if (sl slope >= (sl slope(%column%, %row%) * %.slope cutoff value%))
  % from cell grid% = sl out old(% column%, % row%) + ~
             sl length(%column%, %row%)
else
  % from cell grid% = 0
endif
&end
  /* Select the longest slope length
sl cum l = max(sl north cell, sl NE cell, sl east cell, sl SE cell, ~
         sl south cell, sl SW cell, sl west cell, sl NW cell, ~
         sl high pts)
  /* Kill the temporary grids
kill (!sl north cell sl NE cell sl east cell sl SE cell \sim
    sl south cell sl SW cell sl west cell sl NW cell!)
kill sl out old
  /* Test for the last iteration filling in all cells with data
&sv no data = [show scalar nodata cell]
&if %no data% eq 0 & then
  &sv finished = .TRUE.
  /* Test for any nodata cells
if (isnull(sl cum l) and not isnull(sl outflow))
  sl nodata = 1
else
    sl nodata = 0
```

endif

nodata cell = scalar(0)

docell
 nodata\_cell }= sl\_nodata
end
kill sl\_nodata

&end

/\* Reset original window and clip the cumulative slope length grid \*\*\*\*\*\*\*\*\* setwindow sl\_DEM rename sl\_cum\_l sl\_out\_old sl\_cum\_l = sl\_out\_old kill sl\_out\_old

&return

#### <u>ls.aml</u>

```
/* Grids used from sl.aml:
   /* sl cum l
   /* sl slope
 /* Grid produced for sl.aml:
   /* ls amount
&if %.grid units% eq METERS &then
 ls length = sl cum 1 div 0.3048
&else
 ls length = sl cum l
/* For cells of depostion
if (ls length eq 0)
 ls amount = 0
 /* For slopes 5% and over
else if (sl slope \geq 2.862405)
 ls amount = pow((ls length div 72.6), 0.5) * ~
    (65.41 * \text{pow}(\sin(\text{sl slope div deg}), 2) + \sim
     4.56 * \sin(\text{sl slope div deg}) + 0.065)
 /* For slopes 3% to less than 5%
else if ((sl slope \ge 1.718358) and (sl slope < 2.862405))
 ls amount = pow((ls length div 72.6), 0.4) * ~
     (65.41 * pow(sin(sl slope div deg), 2) + \sim
     4.56 * \sin(\text{sl slope div deg}) + 0.065)
 /* For slopes 1% to less than 3%
else if ((sl slope \geq 0.572939) and (sl slope < 1.718358))
 ls amount = pow((ls length div 72.6), 0.3) * ~
```

&return